

Nuclear modification factor in intermediate-energy heavy-ion collisions

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The transverse momentum dependent nuclear modification factors (NMF), namely R_{CP} , is investigated for protons produced in Au + Au at 1A GeV within the framework of the isospin-dependent quantum molecular dynamics (IQMD) model. It is found that the radial collective motion during the expansion stage affects the NMF at low transverse momentum a lot. By fitting the transverse mass spectra of protons with the distribution function from the Blast-Wave model, the magnitude of radial flow can be extracted. After removing the contribution from radial flow, the R_{CP} can be regarded as a thermal one and is found to keep unitary at transverse momentum lower than 0.6 GeV/c and enhance at higher transverse momentum, which can be attributed to Cronin effect.

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I. INTRODUCTION

Recently, the nuclear modification factor (NMF) has been extensively investigated for different particles at various collision energies in relativistic heavy-ion collisions (HIC) [1–4]. These studies indicate that the NMF, which can be represented either by the modification factor between nucleus-nucleus (AA) collisions and proton-proton (pp) collision R_{AA} or the one between the central collisions and peripheral collisions R_{CP} , is very useful for the study of the quantitative properties of the nuclear medium response when the high speed jet transverses it. In high transverse momentum (p_T) region, NMF is suppressed owing to jet quenching effect in hot-dense matter and thus has become one of the robust evidences on the existence of the Quark-Gluon-Plasma [5, 6]. In lower p_T region, radial flow boosts or the Cronin Effect [7] competes with the quenching effect and enhances the NMF, which has been also demonstrated by the Relativistic Heavy-Ion Collider (RHIC) beam energy scan (BES) project [8].

Meanwhile, collective motion plays an important role in the time evolution of particles, which has been studied over a wide range of collision energy in heavy-ion collision. Around 1A GeV incident energy in central HIC, the colliding nuclei are expected to be stopped and lead to densities of $2 \sim 3\rho_0$ (ρ_0 is the normal nuclei density) at the largest compression time [9]. At this point, high excitation energy stage is reached and some parts of the excitation energy are converted into collective motion, such as radial flow [10, 11]. Thus, in the following expansion stage, the products move outward containing both the collective motion and the thermal motion. It will be of highly interesting to decouple these two parts,

because each of them reflects important information of the HIC process. Efforts have been made by the Blast-Wave model [12–14], and the collective motion parameter (radial flow velocity) together with the thermal motion parameter (temperature) can be extracted at the same time.

Nevertheless, till now, NMF has not been investigated in intermediate energy HIC yet to our knowledge. In particular, the R_{CP} shape will be strongly affected by the radial flow which plays a significant role in the expansion stage especially for the low p_T particles. In order to understand the properties of the nuclear medium response, one may want to know what the behavior of R_{CP} without the contribution from radial flow might be. In the present paper, we address NMF in intermediate energy HIC to study the properties of nuclear medium for the first time. After removing the contribution from the radial flow, the NMF can be regarded as a thermal one, which reflects property of thermal medium produced in intermediate energy HIC. The R_{CP} for emitted protons in Au + Au collision at 1A GeV is investigated systematically.

The article is organized as follows: A brief introduction about the IQMD model is given in Sec. II. In Sec. III, we compare the kinetic energy spectra of light fragments obtained by the IQMD with the one from the EOS experimental result, then we fit the proton transverse mass (m_T) spectra with the Boltzmann function and with the distribution function from Blast-Wave model. In Sec. IV, we show the results of NMFs and compare them with the results extracted from the KaoS experimental data. Finally, the thermal R_{CP} is recalculated by removing the contribution from radial flow. Summary and conclusion are presented in Sec. V.

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II. BRIEF DESCRIPTION OF IQMD MODEL

The Quantum Molecular Dynamics model is a transport model which is based on a many body theory to describe heavy ion collisions from low (dozens of MeV) to relativistic energy [15–18]. The Isospin dependent Quantum Molecular model (IQMD), was extended from the QMD model, with considering the isospin effects. In the past decades, many applications have been successfully performed into nuclear physics studies with the help of IQMD. For instance, IQMD has been successfully applied to treat collective flow, multi-fragmentation, isospin effects in HIC, transport coefficient in HIC, giant resonance, and strangeness production etc [19–23]. In the IQMD model, the wave function of each nucleon is described as a coherent state with the form of Gaussian wave packet,

$$\phi_i(\vec{r}, t) = \frac{1}{(2\pi L)^{3/4}} \exp\left(-\frac{(\vec{r} - \vec{r}_i(t))^2}{4L}\right) \exp\left(\frac{i\vec{r} \cdot \vec{p}_i(t)}{\hbar}\right). \quad (1)$$

Here r_i and p_i are the time dependent variables which describe the center of the packet in coordinate and momentum space, respectively. The parameter L , related to the width of wave packet in coordinate space, is determined by the size of reaction system, i.e. $L = 1.08 \text{ fm}^2$ for Ca+Ca system and $L = 2.16 \text{ fm}^2$ for Au+Au system in this work. The wave function of the system is the direct product of all the nucleon wave functions without considering the Fermion property of nucleon:

$$\Phi(\vec{r}, t) = \prod_i \phi_i(\vec{r}, t). \quad (2)$$

As a compensation, Pauli blocking is employed in the initializations and collision process to restore some parts of the quantum property of many Fermion system.

By applying a generalized variational principle on the action of the many-body system, one can get the equations of motion for p_i and r_i , which are listed as follows

$$\vec{p}_i = -\frac{\partial \langle H \rangle}{\partial \vec{r}_i}; \vec{r}_i = \frac{\partial \langle H \rangle}{\partial \vec{p}_i}. \quad (3)$$

The Hamiltonian $\langle H \rangle = \langle T \rangle + \langle V \rangle$ where T is the kinetic energy, the potential V is expressed by

$$\langle V \rangle = \frac{1}{2} \sum_i \sum_{j \neq i} \int f_i(\vec{r}, \vec{p}, t) V^{ij} f_j(\vec{r}', \vec{p}', t) d\vec{r} d\vec{r}' d\vec{p} d\vec{p}'. \quad (4)$$

In the above, the Wigner distribution function $f_i(\vec{r}, \vec{p}, t)$, which is the phase-space density of the i th nucleon, is obtained by applying the Wigner transformation on the single nucleon wave function:

$$f_i(\vec{r}, \vec{p}, t) = \frac{1}{(\pi \hbar)^3} e^{-(\vec{r} - \vec{r}_i(t))^2 \frac{1}{2L}} e^{-(\vec{p} - \vec{p}_i(t))^2 \frac{2L}{(\hbar)^2}}. \quad (5)$$

The baryon-potential consists of the real part of the G-Matrix which is supplemented by the Coulomb interaction between the charged particles. The former one can

be divided into three parts, the Skyrme-type interaction, the finite-range Yukawa potential, and the momentum-dependent interaction (MDI) parts. The two-body interaction potential V^{ij} in Eq. 4 can be expressed as follows:

$$\begin{aligned} V^{ij} &= G^{ij} + V_{Coul}^{ij} = V_{Skyrme}^{ij} + V_{Yuk}^{ij} + V_{MDI}^{ij} + V_{Coul}^{ij} \\ &= t_1 \delta(\vec{x}_i - \vec{x}_j) + t_2 \delta(\vec{x}_i - \vec{x}_j) \rho^{\gamma-1}(\vec{x}_i) \\ &\quad + t_3 \frac{\exp(-(\vec{x}_i - \vec{x}_j)/\mu)}{(\vec{x}_i - \vec{x}_j)/\mu} \\ &\quad + t_4 \ln^2[1 + t_5(\vec{p}_i - \vec{p}_j)^2] \delta(\vec{x}_i - \vec{x}_j) \\ &\quad + \frac{Z_i Z_j e^2}{\vec{x}_i - \vec{x}_j}. \end{aligned} \quad (6)$$

The symmetry potential between protons and neutrons corresponding to the Bethe-Weizsacker mass formula can be taken as

$$V_{sym}^{ij} = t_6 \frac{1}{\rho_0} T_{3i} T_{3j} \delta(r_i - r_j) \quad (7)$$

with $t_6=100 \text{ MeV}$. By integrating Skyrme part as well as the momentum dependent part of the two-body interaction and introducing the interaction density,

$$\rho_{ij} = \frac{1}{(4\pi L)^{3/2}} \sum_{j \neq i} \exp\left[-\frac{(\vec{r}_i - \vec{r}_j)^2}{4L}\right], \quad (8)$$

one can get the local mean field potential which contains the Skyrme potential and momentum dependent potential

$$U = \alpha \left(\frac{\rho}{\rho_0}\right) + \beta \left(\frac{\rho}{\rho_0}\right)^\gamma + \frac{\rho}{\rho_0} \int d\vec{p}' g(\vec{p}') \delta \ln^2[\epsilon(\vec{p} - \vec{p}')^2 + 1], \quad (9)$$

where ρ_0 is the saturation density at ground state, $g(\vec{p}, t) = \frac{1}{(\pi \hbar)^{3/2}} \sum_i e^{-(\vec{p} - \vec{p}_i(t))^2 \frac{2L}{(\hbar)^2}}$ is the momentum distribution function, the interaction density $\rho = \sum_{ij} \rho_{ij}$, and α , β , and γ are the Skyrme parameters, which connect tightly with the EOS of the bulk nuclear matter, as listed in Table I.

TABLE I: Parameter sets for the nuclear equation of state used in the IQMD model. S and H represent the soft and hard equation of state, respectively, M refers to the inclusion of momentum dependent interaction. This table is adapted from [15].

	α (MeV)	β (MeV)	γ	δ (MeV)	ϵ ($\frac{c^2}{(GeV)^2}$)
S	-356	303	1.17	-	-
SM	-319	320	1.14	1.57	500
H	-124	71	2.00	-	-
HM	-130	59	2.09	1.57	500

With the help of coalescence mechanism, the information of fragments produced in HICs can be identified in IQMD. A simple coalescence rule to form a fragment is used with the criteria $\Delta r = 3.5 \text{ fm}$ and $\Delta p = 300 \text{ MeV}/c$ between two considered nucleons.

III. TRANSVERSE MASS SPECTRA

The Au+Au collisions at 1A GeV are simulated with the IQMD model for both the soft equation of state with MDI (SM) and the hard equation of state with MDI (HM). In order to test the reliability of the model, the kinetic spectra of proton, deuteron and triton obtained by the IQMD with the above equation of state situations are compared with the EOS experimental data in Fig 1 [12]. The conditions of the chosen fragments in our model calculations are $b \leq 3fm$, $\theta_{cms} = 90 \pm 15^\circ$, which are the same as the EOS experimental situation. As shown in Fig 1, the solid lines are the spectra extracted from the IQMD with soft and MDI potential, and the dash lines are the spectra extracted with HM potential. From Fig. 1, we find that both the soft and hard equation of state situation can essentially describe the EOS experimental data nicely. A little higher yield of protons and lower yield of t are observed in the case of the HM potential. The enhanced yield of protons can be attributed to stronger mean field interaction in HM case compared to that in SM case.

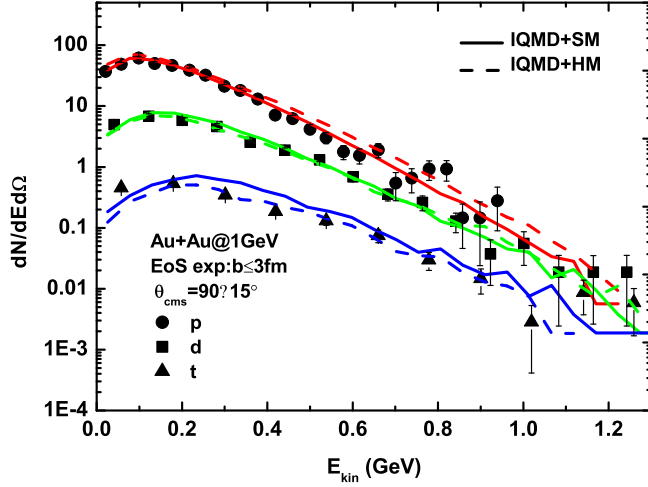


FIG. 1: (Color online) E_{kin} spectra of proton (circle), deuteron (square), triton (triangle) in Au + Au at 1A GeV. The solid symbols are the experimental data from the EOS collaboration [12], and the solid line is our IQMD simulation with the soft+MDI potential, and the dash line is for the hard+MDI potential.

Transverse mass m_T , is given by $m_T = \sqrt{p_T^2 + m_0^2}$, with the rest mass of protons m_0 . Fig. 2 shows our simulation results for the double differential transverse mass spectra ($\frac{d^2N}{2\pi m_T dm_T dy}$) of protons at different centralities (0–10%, 10–20%, 20–40%, 40–60%, 60–80%) together with two fit results either from Boltzmann distribution function or from Blast-Wave model distribution function in the framework of IQMD model with SM potential. The c.m.s. rapidity cut is $|Y/Y_{proj}| < 0.1$ where Y_{proj} is the initial projectile rapidity. At the end of this section, a discussion will be given for the fit parameters, i.e.

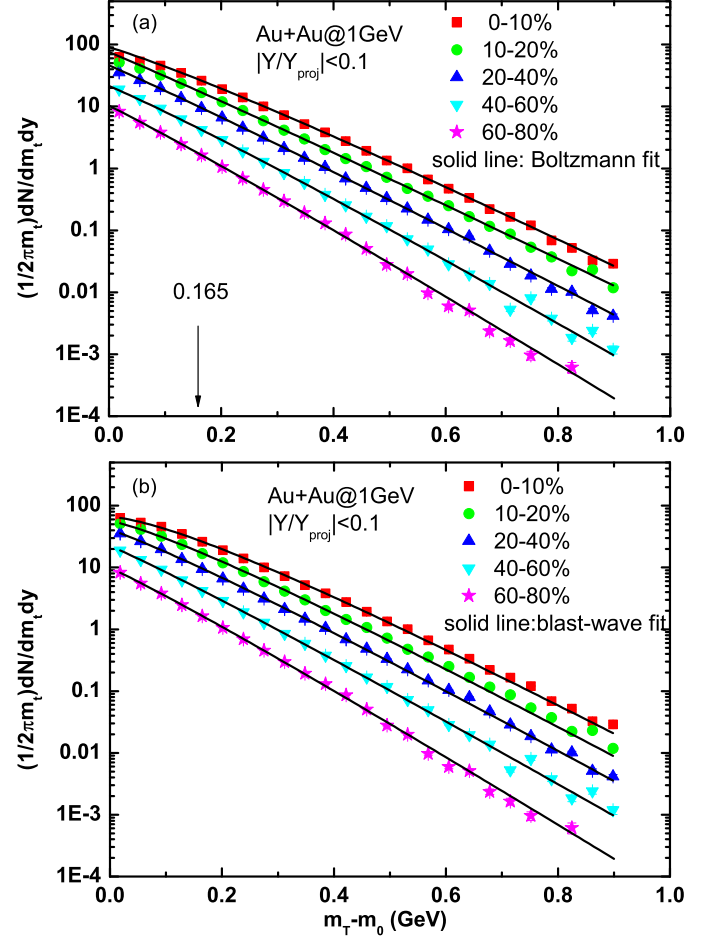


FIG. 2: (Color online) m_T spectra of protons at different centralities (0-10%,10-20%,20-40%,40-60%,60-80%) for Au + Au at 1A GeV from IQMD+SM simulation, the upper panel is the Boltzmann fit in the range of $m_T > 0.165$ GeV, and the lower panel is the Blast-Wave fit.

temperature and radial flow.

A. The Boltzmann fit

In heavy-ion collisions, particles collide with each other randomly, which can be described in term of thermal motion [24]. Lots of works demonstrate that the Boltzmann distribution can roughly describe the particle spectra by a thermal source in HICs [25–28]. If the particles are ejected from a single pure high temperature thermal source, its transverse mass spectra should satisfy the Boltzmann distribution function, i.e. $dN/(dm_T dy) \approx f(m_T) \cdot \exp(-m_T/T)$, which is close to a straight line when the y-axis is plotted logarithmically. The results of the m_T spectra of protons fitted with the Boltzmann function are shown in Fig. 2(a). The proton spectra at different centralities are fitted by the Boltzmann function in the region of $m_T > 0.165$ GeV and extrapolated

to the low m_T region. It is interesting to find that the spectra in central collisions have an obvious “shoulder”-like structure in the low m_T region while there is no such structure for peripheral collisions. This means the spectra in central collisions deviate from the Boltzmann distribution in the low m_T region, which can be essentially attributed to the radial flow in central collisions. The fit parameters of the slope temperature are listed in the second column of Table II. From peripheral to central collision the slope temperature extracted from the Boltzmann function fit shows a decreasing trend, which is very different from that extracted from the Blast-Wave model fit as discussed in next section.

TABLE II: Fit parameters: slope temperature T_{slope} from Boltzmann fitting and freeze out temperature T_f from Blast-Wave fit.

Cent.	T_{slope} (MeV)	T_f (MeV)
0-10%	93.06 ± 0.91	61.60 ± 0.81
10-20%	92.67 ± 1.74	62.99 ± 0.98
20-40%	86.55 ± 1.35	64.64 ± 0.89
40-60%	78.50 ± 1.54	64.51 ± 0.76
60-80%	73.87 ± 1.62	60.58 ± 1.05

B. The Blast-Wave fit

Considering that the Boltzmann function cannot fit well the m_T spectra in the low m_T region due to the existence of collective radial flow, we adopt a hydrodynamically inspired “Blast-wave” model to describe the m_T spectra with two free parameters: collective transverse flow velocity β and kinetic freeze-out temperature T_f . In this model, the spectrum is computed by boosting the thermal source both in longitudinal and transverse direction [10, 29]. The radial velocity distribution β_r in the region $0 \leq \beta_r \leq R$ is described by a self-similar profile, which is parameterized by the surface velocity β_S :

$$\beta_r = \beta_S \cdot \left(\frac{r}{R}\right)^\alpha, \quad (10)$$

where R is the freeze-out radius, namely the maximum radius of the expanding source at thermal freeze-out time. β_S is the particles’ radial velocity on the surface of the freeze out volume when $r = R$, and the exponent α represents for the radial flow profile which describes the evolution of the radial flow velocity (when $\alpha = 0$, it means uniform velocity; when $\alpha = 1$, the expansion is similar to Hubble’s law; when $\alpha = 2$, it corresponds to a hydromechanical expansion). The particle spectra are the superposition of individual thermal source at different r , each boosted with the angle $\rho = \tanh^{-1}\beta_r(r)$:

$$\frac{dn}{m_T dm_T} \propto \int_0^R r dr m_T I_0\left(\frac{p_T \sinh \rho}{T_f}\right) K_1\left(\frac{m_T \cosh \rho}{T_f}\right), \quad (11)$$

where K_1, I_0 are the modified Bessel function, T_f is the freeze-out temperature. The spectrum shape is determined by the freeze-out temperature T_f , the velocity of the transverse expansion β_S , the flow velocity profile α and the mass of the particle m_0 . The average flow velocity is estimated by taking an average over the transverse geometry: $\langle \beta_r \rangle = \beta_S \frac{2}{2+\alpha}$.

The spectra of protons can be well described by the Blast-Wave model as shown in Fig. 2(b) and the fit parameters are listed in Table III. Obviously, the whole spectra are well fitted, even for the “shoulder structure” at low m_T in central collisions (for the centralities of 0-10% and 10-20%). From central collisions to peripheral ones, the velocity β_S decreases and while the temperature has only a slight increase [30]. It is noted that the similar trend was also seen in the fitting result in RHIC energy region, which might be owing to non-equilibrium effect in peripheral collision. For example, by replacing the Boltzmann statistics with the Tsallis statistics in traditional Blast-Wave model, the Tsallis Blast-Wave model (TBW) can describe the peripheral spectra well and give a more reasonable fitting result (a low value of β_S and $(q-1) > 0$ at peripheral collisions) [31].

The main results from the fitting of the m_T spectra are following:

1. Radial flow ($\langle \beta_r \rangle$).

In Fig. 2(b), the proton spectra have been described very well with the Blast-Wave model. The average radial flow is about 0.33c in the central collisions (0-10%), and reduces to 0.22c in peripheral collisions (60-80%). This result with a larger radial flow existing in central collisions is consistent with the physics picture of HICs.

In another scenario, the average kinetic energy $\langle E_{kin} \rangle$ of protons, deuterons and tritons at mid-rapidity are consistent with the picture described by the Blast-Wave model. Fig. 3 shows the mass number dependence of $\langle E_{kin} \rangle$. They have a linear relationship: $\langle E_{kin} \rangle = E_{th} + E_{flow} = \eta \cdot A + 3T/2$ where $\eta = 1/\sqrt{1 - \langle \beta_r^2 \rangle} - 1$. The slope is the quantity related to radial flow, and the intercept is the quantity related to thermal temperature. We can also extract the radial flow and temperature information by the linear curve about E_{kin} vs A , the result is listed in the lower part of the Table III, which is comparable with the Blast-Wave fit result.

2. Freeze out temperature (T_f)

We use Boltzmann distribution to fit the proton spectra, with the fitting parameters at different centralities called “slope temperature” listed in Table II. The temperature shows a decreasing trend from 93.06 MeV in central collisions to 73.87 MeV in peripheral collisions. Comparing with the Boltzmann fit results, the freeze-out temperature from the Blast-Wave fit is smaller, and shows a little increasing trend. This difference is owing to that the collective radial flow motion effect has been misunderstood as the thermal part of motion in the Boltzmann description.

3. Flow profile (α)

The α exponent describes the evolution of the radial

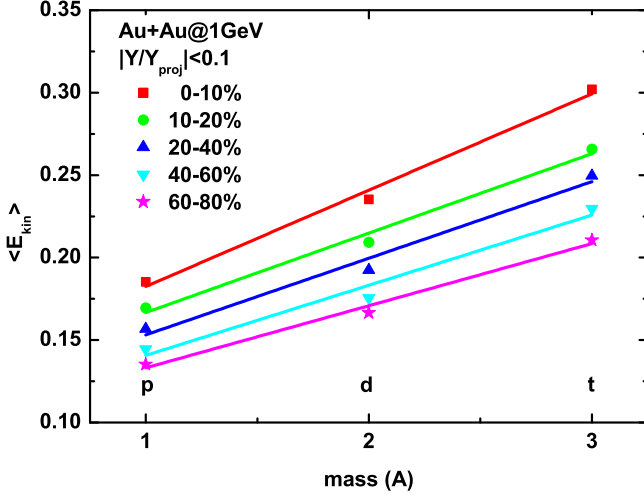


FIG. 3: (Color online) Average E_{kin} of $Z=1$ particle in Au + Au at 1.4 GeV for different centralities (0-10%, 10-20%, 20-40%, 40-60%, 60-80%), the solid line represents the linear fit on $\langle E_{kin} \rangle$ vs A in each centrality, the fit parameters are displayed in Table III

TABLE III: The parameters of radial flow β_S , $\langle \beta_r \rangle$ and the freeze-out temperature T_f at various centralities with different fitting methods. The upper one is from proton m_T spectra described by the Blast-Wave model. The lower one is from fitting the average kinetic energy $\langle E_{kin} \rangle$ of p, d, t, which is displayed in Fig. 3.

	β_S	$\langle \beta \rangle$	T_f (MeV)
Blast-wave			
0-10%	0.3615	0.3309 ± 0.0028	61.60 ± 0.81
10-20%	0.3199	0.2928 ± 0.0037	62.99 ± 0.98
20-40%	0.2798	0.2561 ± 0.0039	64.64 ± 0.89
40-60%	0.2452	0.2241 ± 0.0039	64.51 ± 0.76
60-80%	0.2355	0.2155 ± 0.0056	60.58 ± 1.05
$\langle E_{kin} \rangle$ vs A			
0-10%		0.3275 ± 0.0047	82.72 ± 6.97
10-20%		0.2996 ± 0.0057	79.02 ± 6.93
20-40%		0.2946 ± 0.0070	71.12 ± 8.94
40-60%		0.2752 ± 0.0032	67.52 ± 7.69
60-80%		0.2670 ± 0.0036	63.63 ± 5.27

flow velocity from any radius r ($0 < r < R$). We set the parameter α free in Blast-Wave fit, which is different from some previous works keeping a fixed value equal to 1 or 2 [29, 31, 32] or some assuming a common flow (i.e. $\alpha = 0$) [11, 12, 33, 34]. The α makes a little difference to the fitting value of β_S while the choice of R value have no influence on the fitting which chosen $R = 40$ fm in our work. We get the α value equal to 0.336 on the spectra of 0-10% centrality and fix this value when do the fitting on the other centralities. A similar value of α has been also obtained in Ref. [35] for Au + Au collisions in ultra-relativistic energy.

IV. NUCLEAR MODIFICATION FACTOR

To explore the nuclear medium response, the ratio R_{CP} between the particle yield in central collisions and the particle yield in peripheral collisions, has been introduced. Both yields are normalized by corresponding nucleon-nucleon binary collision numbers $\langle N_{coll} \rangle$ (binary scaling):

$$R_{CP} = \frac{Yield(central)/\langle N_{coll}^c \rangle}{Yield(peripheral)/\langle N_{coll}^p \rangle}, \quad (12)$$

where the yield is the differential invariant yield ($\frac{d^2 N}{2\pi p_T dp_T dy}$). If the nucleus-nucleus collision is a mere superposition of N_{coll} independent nucleon-nucleon collisions, R_{CP} would be unit with p_T . Thus any departures from $R_{CP}=1$ indicate nuclear medium effects or other dynamical effects.

A. The normal NMF

The normal R_{CP} versus p_T is obtained by dividing the p_T spectra in central collisions with the ones in peripheral collisions with taking the respective binary collision number into account. To test the reliability of model, the results from IQMD calculation are compared with that extracted from KaoS experimental data. Following the experimental conditions [26], the central collision events are chosen with charged particle multiplicity $M_z > 50$, and the peripheral collision events with $M_z < 26$. The identified protons are chosen the same as the KaoS experiment, namely, in the polar angle of 40-48 degrees, and the momentum range 0.320-1.440 GeV/c. The spectra of proton in central and peripheral collisions are showed in Fig. 4(a), together with the result from IQMD+SM(HM) representing with different type lines elaborated in figure caption. Results demonstrate that both the soft and hard EOS can describe the experimental data nicely. Shown in Fig. 4(b) is the R_{CP} as a function of total laboratory momentum from IQMD simulation and the KaoS experiment. Two parameter sets of equation of state, namely SM and HM, are employed in IQMD calculation. The R_{CP} of protons from experiment (circle) and from IQMD calculation (solid red line: SM; dash blue line: HM) increase almost linearly with the total momentum in laboratory system (p_{lab}). This is consistent with those behaviors from lower RHIC Beam-Energy-Scan energies, e.g. the R_{CP} for proton in Au+Au at 7.7 A GeV [8], and can be understood by radial boosts and/or the Cronin Effect [7]. The R_{CP} of proton is not so sensitive to the hard or soft equation of state in the IQMD calculations, indicating the multiple collision process dominates here. It's a need to note that the R_{CP} from model are arbitrarily scaled to match with the experimental result owing to the unknown N_{coll} in KaoS experiment.

In IQMD model, two particles collide if the minimum relative distance of their centroids of the Gaussian wave

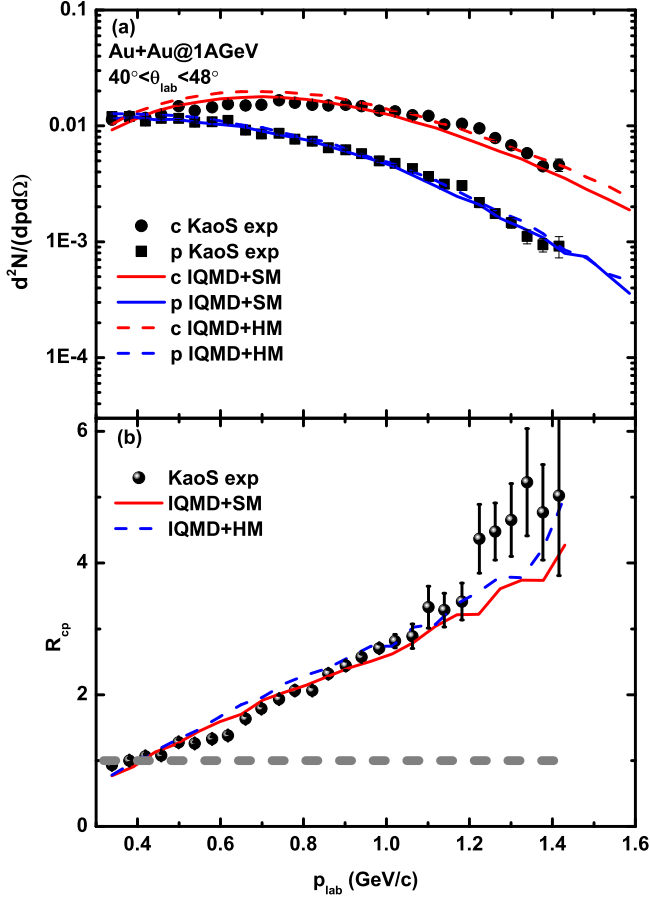


FIG. 4: (Color online) a) The central and peripheral spectra of protons taken from the KaoS experimental data [26] are compared with our IQMD simulations with SM and HM interaction parameters. The character “c” (“p”) represents central (peripheral) collision, circle (square) represents the KaoS experimental result, solid red (blue) line represents IQMD with SM interaction and dash red (blue) line IQMD with HM interaction. Central (circle symbol) and peripheral (square symbol) collisions are selected by the charge particle multiplicity, namely $M_z > 50$ and $M_z \leq 26$. b) Experimental R_{CP} (circle) calculating from the KaoS experimental data is compared with IQMD with SM (solid red line) and HM (dash blue line) results. The dash line ($R_{CP}=1$) is just guiding the eyes.

during their motion, in the CM frame fulfills the requirement:

$$d \leq d_0 = \sqrt{\frac{\sigma_{tot}}{\pi}}, \quad (13)$$

where the cross section σ_{tot} is assumed to be the free cross section of the regarded collision type (N-N, N- Δ , etc.). In this work, the collision numbers in every centralities are counted with the “ N_{collt} ” counter when each collision occurs. For each collision the phase space densities in the final states are checked in order to assure that the final distribution in phase space is in agreement with the Pauli principle, the Pauli blocking number has

been counted by the “ N_{paubl} ” counter. Then, we can get the real collision number ($N_{coll} = N_{collt} - N_{paubl}$). For Au+Au collision at incident energy 1A GeV, the average collision numbers are 242.5, 473, 795.5, 1136, 1463 in five centralities from peripheral to central collisions in our IQMD model, respectively.

The R_{CP} versus p_T shows centrality dependence. In Fig. 5(a), four cases at different centralities are investigated, which are $\frac{0-10\%}{60-80\%}$ (red dot), $\frac{10-20\%}{60-80\%}$ (green square), $\frac{20-40\%}{60-80\%}$ (blue up triangle) and $\frac{40-60\%}{60-80\%}$ (pink downtriangle). From the most peripheral case in numerator (i.e. $\frac{40-60\%}{60-80\%}$) to the most central case in numerator (i.e. $\frac{0-10\%}{60-80\%}$), the R_{CP} becomes more and more p_T dependent. For all these cases, R_{CP} rises with p_T , with a cross point shows up at $p_T = 0.5$ GeV/c, which may suggest a balance between two mechanisms for the p_T dependence of R_{CP} .

On the one hand, in the low p_T region (p_T less than 0.5 GeV/c), radial flow takes a major role in central collisions, which pushes protons to higher p_T region and results in the smaller R_{CP} at low p_T . On the other hand, in the high p_T region (p_T greater than 0.5 GeV/c), the Cronin effect (nucleon multiple scattering effect) [36, 37] tends to transform the longitudinal momentum into the transverse momentum and increase the p_T in central HIC, leading to the larger R_{CP} at high p_T .

B. The thermal NMF

In order to investigate the thermal property of the medium in the collision overlapping region, one needs to deduct the contribution of collective flow to focus on thermal effect. The radial flow parameter extracted by the Blast-Wave fit has been displayed in Table III. By subtracting the radial velocity of each particle, we recalculate the R_{CP} of protons without the radial flow contribution.

To determine the magnitude of radial flow, one needs to figure out the size of freeze-out volume. In the transport model IQMD, a density criterion is applied here. During the expansion process, the stage can be chosen as freeze-out stage, when the density at the center of each collision reaches $1/8\rho_0$. At this stage, all the products (including fragments and free nucleons) cease the strong interaction among them and almost fix their momenta. For the case of Au+Au collision at $E_{beam} = 1A$ GeV, this freeze-out time is about 60 fm/c, and the corresponding radius R_{max} of freeze-out volume is about 40 fm (half of the reducing edge of radius distribution of all emitting protons), which is of course model dependent. Fig. 5(b) shows the NMF of protons inside the freeze-out volume. In comparison with Fig. 5(a), freeze-out sphere cuts off most of higher p_T protons. Once the freeze-out sphere is fixed, the radial flow β_r for the particles inside the volume can be calculated through formula in Eq. (10), here $\alpha = 0.336$ is taken from the Blast-Wave fit for the

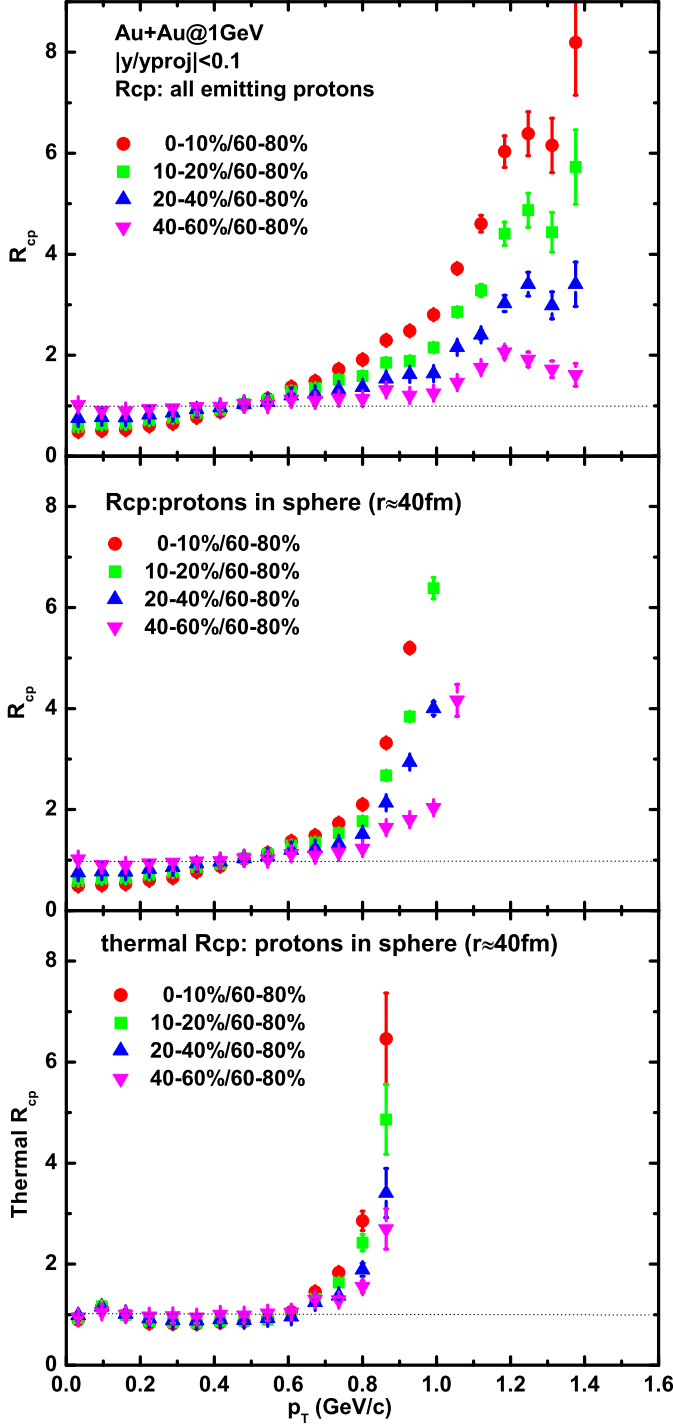


FIG. 5: (Color online) Nuclear modification factor, R_{CP} of protons in Au + Au at 1A GeV. The panel (a) is the original R_{CP} , the panel (b) is the R_{CP} inside the freeze-out sphere, and the panel (c) shows the R_{CP} (b) after deducting the radial flow effect from the panel (b), which is named as the thermal R_{CP} . The dot line ($R_{CP}=1$) is just guiding the eyes.

p_T spectra. The contribution of radial flow on p_T is the projection of radial momentum ($p_r = m_0 \cdot \beta_r \cdot \gamma_r$) on the p_T vector, and the thermal transverse momentum is $p_T = p_T - \frac{p_r \cdot p_T}{|p_T|}$. The thermal R_{CP} is then obtained by dividing the thermal p_T distribution in central collisions to that in the peripheral collisions with taking the respective binary collision number into account, which is shown in the Fig. 5(c). It is found that the thermal R_{CP} becomes almost unitary below 0.6 GeV/c, which illustrates that the original increasing R_{CP} behavior in low p_T region essentially stems from the collective radial flow effect, and the thermal motion of nucleus-nucleus collision can be seen as the independent overlap of nucleon-nucleon collisions. It is also noted that the thermal R_{CP} is larger than 1 at p_T above 0.6 GeV/c, where the Cronin effect plays a dominant role for the R_{CP} increasing behavior versus p_T [7, 36].

V. CONCLUSION

In summary, the nuclear modification factor has been introduced in intermediate energy HIC in the framework of transport model, and thermal NMF has been proposed. First, we test the reliability of the IQMD model by comparing the kinetic energy spectra of light fragments (p, d, t) obtained by the IQMD model with the EOS experimental data, and we found the model can describe the data nicely. Secondly, the transverse mass spectra of protons are fitted by the Boltzmann distribution function as well as the distribution function from Blast-Wave model. It is found that the latter gives a satisfying description of the transverse mass m_T spectra of protons at freeze-out time, which demonstrates that the kinetic energy of protons contains the collective radial motion part and random thermal motion part. The fitting radial flow parameter β_s and temperature parameter T_f are consistent with the results from the EOS collaboration [12] and the FOPI collaboration [13, 14]. While, the Boltzmann description overestimates the proton yield at low m_T , because of the missing radial flow contribution. Thus the fit temperature from the Boltzmann description can be interpreted as the apparent temperature of the emission source, which decreases from the central collisions to the peripheral collisions. It is found that both the radial flow effect and Cronin effect play their corresponding roles in shaping the p_T dependence of R_{CP} . The radial flow magnitude can be extracted by fitting the m_T spectra with the distribution function from Blast-Wave model. The thermal modification factor is then obtained by removing the contribution from the radial flow. It is found that the thermal R_{CP} of protons is close to 1 at lower p_T , where protons emitted from Au+Au collisions can be regarded as independent superposition of emitted protons by nucleon-nucleon collisions, and while R_{CP} enhances at higher p_T , where the Cronin effect, i.e. multiple production mechanism of protons plays an increasing role. On the other hand, in light of this study, the nuclear modifi-

cation factor at very high p_T which has been often used to investigate jet-quenching effect at RHIC and LHC energies was actually nearly not affected by the collective radial flow.

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